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(54) Title: RADIATION SOURCE (57) Abstract An improved radiation source, exploiting the spontaneous radiation generated from the interaction of an electron beam and a conductive grating. Conditions are defined for generating coherent or noncoherent radiation, and for extending the tunability of the radiation source from millimeter, IR, visible and UV wavelengths to x-ray wavelengths, and for generating multiple wavelengths simultaneously. Conditions are disclosed for enhancing the intensity of the spontaneous radiation, and for modulating the radiation		

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RADIATION SOURCE

1 BACKGROUND OF THE INVENTION

The present invention relates to radiation sources employing an electron beam reflecting from a conductive grating.

5 Radiation from electrons interacting with a diffraction grating has been studied both theoretically and experimentally since the early work of W. W. Salisbury described in U.S. Patent No. 2,634,372 and in J. Opt. Soc. Am., Vol. 60, page 1279 et seq. (1970), and the
10 work of S. J. Smith and E. M. Purcell as described in Phys. Rev., Vol. 92, page 1069 et seq. (1953). As described in these references, an electron beam
15 interacting with the surface of a metallic grating has been shown to generate electromagnetic radiation. This radiation source is easily tunable, with the wavelength
λ depending on the grating period a, electron speed v₀ and the angle θ between the electron velocity and observation direction as shown in Equation 1, where c is the velocity of light.

20

$$\lambda = a \left(\frac{c}{v_0} - \cos(\theta) \right) \quad (1)$$

1 Past theoretical treatments of the radiation from
an electron beam interacting with the surface of a
metallic grating are understood to have assumed that
the electrons do not collide with the grating. With
5 this assumption, both incoherent and coherent radiation
have been discussed.

 The incoherent radiation has been discussed in
terms of dipole radiation from oscillating image charges
(S. J. Smith and E. M. Purcell, Physics Review, Vol.
10 92, page 1069 (1953)), grating scattering of the
evanescent waves tied to the electrons (E. Labor,
Physics Review, Vol. A7, page 435 (1973); G. Toraldo di
Francia, Nuovo Cimento, Vol. 16, page 61 (1960)), and
rigorous Green's function formulations of the
15 electromagnetic fields generated in the half-space
grounded by the grating (C. W. Barnes and K. G. Dedrick,
J. Appl. Phys., 37, 411 (1966); P. M. Van den Berg and
T. H. Tan, J. Opt. Soc. Am., 64, 325 (1974)).

 The generation of coherent radiation has been
20 discussed in connection with the situation when the
electron beam and grating are placed within a resonant
cavity. The resulting device has been called the
oratron or ledatron. (F. S. Rusin and G. D. Bogomolov,
JETP Lett., 4, 160 (1966); K. Mizuno, S. Ono, and Y.
25 Shibata, IEEE Trans. Electron Devices, ED-20,749 (1973)).
In that case, the coherent radiation produced has been
treated by calculating the power transferred from an
electron beam to a cavity mode which is perturbed by
the periodic grating. R. P. Leavitt, D. E. Wortman,
30 and C. A. Morrison, Appl. Phys. Lett., 35, 363 (1979);
R. P. Leavitt and D. E. Wortman, J. Appl. Phys., 54,
2219 (1983).

1 In none of the foregoing analyses are the electrons
assumed to collide with the grating. There is, however,
some experimental work indicating that electron collisions
with the grating should make an appreciable difference.

5 The early experiments of W. Salisbury with low divergence
beams scattering off the grating, discussed in the
paper "Generation of Light from Free Electrons", Winfield
W. Salisbury, Journal of the Optical Society of America,
Winfield W. Salisbury, Vol. 60, No. 10, Oct. 1970, pp.

10 1279-1284, disclosed the following significant differences
from the Smith-Purcell-type experiments in which no
electron collisions with the grating occurred.

1. The radiation intensity was much larger with
very bright colors appearing even when overhead
15 illumination was present;

2. electrons which were 1 mm from the grating
contributed as much as electrons within a grating
spacing of the grating; and

3. the radiation intensity was largest when the
20 numbers of scattered and unscattered electrons were
comparable.

The second finding above is in direct contradiction
to theoretical calculations which assume that no
collisions with the grating occur. These calculations
25 indicate that electrons which are farther away from the
grating than one grating spacing should produce negligible
radiation.

Insofar as is known to applications, the above-
referenced research efforts have not resulted in
30 explanations of the underlying radiation phenomena,
which has, in turn, limited the usefulness of the
phenomena.

1 It is, therefore, an object of the present
invention to provide radiation source resulting from an
understanding of the emission of radiation from the
reflection of electrons from a grating.

5 It is another object of the present invention to
provide a radiation source which is easily tunable over
a broad band of wavelengths and which can provide either
coherent or noncoherent radiation.

10 It is another object to provide a radiation source
which may be easily modulated both in frequency and in
amplitude.

SUMMARY OF THE INVENTION

15 An improved radiation source is disclosed. The
radiation source comprises a conductive grating having
a periodic grating spacing a , means for providing a
periodic space-charge structure of electrons above the
grating, and an electron beam generator adapted to
20 direct a beam of electrons through the periodic space-
charge structure. Radiation is emitted, resulting from
the accelerated surface currents induced in the grating
by the electron beam and space-charge structure. The
radiation passes through the periodic space-charge
25 structure, a slow wave radiation structure, wherein the
spatial sidebands move more slowly than the fundamental
wavelength radiation. This allows resonant transfer of
energy between the electrons and the slowly moving
component of the radiation, thus, amplifying the
radiation from the induced grating surface currents.

30 In accordance with the invention, coherent
radiation from the device will dominate the incoherent
radiation when the spontaneous radiation from the
induced surface currents experience an amplification
gain greater than unity on moving through the periodic
35 space-charge structure above the grating.

1 Another aspect of the invention is the enhancement
of the coherent radiation using collective effects.
This occurs when the plasma frequency of the electron
beam is comparable to the radiation frequency. Equation
5 1 shows that the latter is of the order of v_0/a , where
 v_0 is the electron velocity and a is the grating spacing.

In an alternative embodiment, the periodic space-
charge structure is created by means other than by
scattering an electron beam off a diffraction grating,
10 i.e., by use of a Periodic Pierce electrode structure to
create sheets of charged particles transverse to the
beam, as well as to create induced surface currents.

In another alternate embodiment, the radiation
source is disposed in a cavity comprising a reflecting
15 surface constructed of a superconducting material,
which is operated at a superconducting temperature.
This results in the reflecting surface becoming almost
loss-free, thus permitting the resonant fields to
increase so that more energy can be transferred between
20 the beam electrons and the field. The cavity may
alternatively be constructed so that the reflecting
faces are disposed to capture the radiation at a
predetermined angle to maximize the radiation.

In another embodiment, the radiation source is
25 adapted to enhance radiation in a particular direction,
by appropriate selection of the grating blaze angle and
depth.

Radiation at different wavelengths and with
correlated phases can be radiated simultaneously by
30 employing multiple beams of electrons of different
energies.

1 The radiation emitted by the radiation source in
accordance with the invention can be both frequency-
modulated and amplitude-modulated, the former by varying
the electron acceleration voltage and the latter by
5 deflecting the beam transversely. Transverse deflection
can be achieved by applying a small voltage to the
grating.

 The invention may be extended to x-ray wavelengths,
by using crystals or superlattices to either reflect or
10 transmit charged particles to create periodic sheets of
space charge. Broadband radiation may be obtained by
directing the beam more directly at the grating, so
that a significant number of the high energy electrons
are absorbed into the grating, resulting in generation
15 of significant Bremsstrahlung radiation.

BRIEF DESCRIPTION OF THE DRAWINGS

 These and other features and advantages of the
present invention will become more apparent from the
20 following detailed description of an exemplary embodiment
thereof, as illustrated in the accompanying drawings,
in which:

 FIG. 1 is a general schematic diagram of a
radiation source which employs the interaction of an
25 electron beam and a grating.

 FIG. 2 is a graph which compares the angular
distribution of the Smith-Purcell-type radiation density
derived in accordance with the invention (solid curve)
with the values obtained by known Green's function
30 formulations (dashed curve).

 FIG. 3 illustrates a simple model of the
structure for generating Salisbury-type radiation.

1 FIGS. 4a-4c are graphs plotting the energy
transfer from electrons to the radiation field in
accordance with the invention for representative
parameters.

5 FIGS. 5a and 5b show simplified diagrams of
an alternate embodiment of the invention, wherein the
periodic space-charge structure is created by an
accelerating grid structure oriented so as to inject
sheets of electrons transverse to the radiating electron
10 beam.

FIG. 6 is a diagram of a radiation source
employing a cavity in accordance with the invention.

15 FIG. 7 is a simplified schematic drawing of
a radiation source employing a cavity with a superconducting
reflecting surface to increase the intensity of the
emitted radiation.

FIG. 8 is a diagram of a radiation source
mounted in a cavity with reflecting faces adapted to
capture radiation at predetermined angles.

20 FIG. 9 is a simplified schematic view of a
radiation source employing a planar mirror.

25 FIGS. 10a-10d are graphs illustrating
respectively the relationship between the observation
angle and the amplitude of induced surface current
radiation, the gain resulting from the space-charge
structure and the product function of the amplitude and
amplification functions, for a radiation source in
accordance with the invention.

30 FIGS. 11a and 11b are simplified diagrams
of features of a radiation source in accordance with
the invention, wherein a crystalline and superlattice
structure are respectively employed as the grating.

1 DETAILED DESCRIPTION OF THE PREFERRED EMBODIMENTS

 The present invention comprises a novel radiation
source. The following description is presented to
enable any person skilled in the art to make and use
5 the invention. Various modifications to the preferred
embodiments will be readily apparent to those skilled
in the art, and the generic principles defined herein
may be applied to other embodiments and applications.
Thus, the present invention is not intended to be
10 limited to the embodiments shown, but is to be accorded
the widest scope consistent with the principles and
novel features disclosed herein.

 The invention comprises a radiation source
employing the interaction of an electron beam with a
15 conductive grating. FIG. 1 discloses a simplified
schematic diagram of the system. The elements are
enclosed in chamber 20, which is evacuated preferably
to a pressure of about 10^{-3} Torr or below. The conductive
grating 10 is disposed in the chamber 20, mounted on
20 adjusting screws 15 which permit translating and tilting
of the grating position from outside the vacuum chamber.

 An electron beam gun 30 is disposed within chamber
20 and is adapted to generate an electronic beam 40.
In the disclosed embodiment, the gun 30 is a Pierce
25 electron gun, comprising a thermionic cathode 32 as a
source of free electrons, an accelerating grid 34 and
collimating plates 36 for collimating the resultant
electron beam 40. The acceleration voltage is adjustable.
(In experiments conducted by applicants, acceleration
30 voltages up to 150 kV have been used and higher
accelerations would be beneficial in some applications.)

1 The electron beam 40 is directed over the grating
10. The distance between the beam and the grating, and
the beam incidence angle, can be adjusted by translating
and tilting the grating from outside the vacuum chamber.
5 An electron catcher 50 is disposed in the chamber,
opposite the grating from the electron gun so as to
trap the unscattered electrons after passing the grating.

Windows 60 are provided in the enclosure defining
the evacuated chamber 20 for escape of the radiation 70
10 generated by the electron beam.

A. Spontaneous Radiation.

1. Smith-Purcell-Type Radiation When Electrons Do Not
Collide With Grating.

15 As was discussed above, several theoretical
discussions have appeared in the literature concerning
the case with no electron collisions with the grating.
This is the case when the electron beam 40 as shown in
FIG. 1 is not allowed to graze the grating 10. These
20 discussions range from the original idea of Smith and
Purcell of dipole radiation from an oscillating image
charge in the grating, though calculations of the
scattering from the grating of the evanescent waves
tied to the electrons, to rigorous Green's function
25 formulations of the electromagnetic fields generated in
the region bounded by the conduction grating. (S. J.
Smith and E. M. Purcell, Phys. Rev., 92, 1069 (1953);
E. Labor, Phys. Rev., A7, 435 (1973); G. Toraldo di
Francia, Nuovo Cimento, 16, 61 (1960); C. W. Barnes and
30 K. G. Dedrick, J. Appl. Phys., 37, 411 (1966); P. M.
Van Den Berg and T. H. Tan, J. Opt. Soc. Am., 64, 325
(1964)).

1 The angular distribution of the radiation intensity
 predicted by the simple oscillating image charge analog
 is quite different from that predicted by the rigorous
 Green's function calculations. The former gives a
 5 characteristic dipole radiation pattern with the major
 lobes in the directions defined by the electron path;
 as the electron energy increases, the lobe in the
 direction of the electron's motion increase, while the
 backward lobe decreases, (W. W. Salisbury, U.S. Patent
 10 No. 2,634,372 (1949); W. W. Salisbury, J. Opt. Soc.
Am., 60, 1279 (1970)). On the other hand, the Green's
 function approach appears to give the main lobe in the
 backward direction. (P. M. Van den Berg, J. Opt. Soc.
Am., 63, 1588 (1973)). The results of the rigorous
 15 Green's function treatments are expressed in terms of
 perturbation expansions, and these are sufficiently
 complex that the underlying physical occurrences can be
 obscured.

One aspect of the invention is the provision of a
 20 simple model of the radiation mechanism which emphasizes
 the underlying physics and illustrates why the image
 charge and Green's function approaches lead to such
 different results.

An approximate expression may be obtained for the
 25 surface current density $\vec{j}(\vec{r}, t)$ induced in the grating
 by a passing electron. In terms of this current density,
 the ω frequency component of the vector potential \vec{A}_ω at
 a large distance R_0 from the grating in the direction
 $\vec{k}/|\vec{k}|$ is given by:

$$30 \quad \vec{A}_\omega = \frac{e^{ikR_0}}{2\pi c R_0} \iint dt dS e^{i(\omega t - \vec{k} \cdot \vec{r})} \vec{j}(\vec{r}, t) \quad (2a)$$

- 1 where c is the speed of light, $k = \omega/c$, and dS is the
 differential area element on the grating surface. The
 energy $d\varepsilon_\omega$ radiated into the element of solid angle
 $d\Omega$ in the form of waves with frequencies in the angular
 5 frequency interval $d\omega$ is then:

(2b)

$$d\varepsilon_\omega = c |\vec{k} \times \vec{A}_\omega|^2 \frac{R_0^2}{(2\pi)^2} d\Omega d\omega$$

10

- The surface current density $\vec{j}(\vec{r}, t)$ can be approximated
 by modifying slightly that which would result from an
 electron moving parallel to a flat conductor. Thus,
 for an electron of charge e at a distance l above a
 15 flat conductor, the surface charge density at a radial
 distance P from the point immediately below the electron
 is:

(3)

$$\sigma_0(P, l) = \frac{el}{2\pi(P^2 + l^2)^{3/2}}$$

20

If the undulating geometry of the diffraction
 grating is added as a simple sinusoidal perturbation
 of wave number \vec{k}_g and amplitude b , the surface charge
 density can be approximated by:

(4)

25

$$\sigma(P, l + b e^{i\vec{k}_g \cdot \vec{r}}) = \sigma_0 + \frac{\partial \sigma_0}{\partial l} b e^{i\vec{k}_g \cdot \vec{r}}$$

The corresponding perturbed surface currents will be:

(5)

30

$$j_x = \frac{\partial \sigma_0}{\partial l} b e^{i\vec{k}_g \cdot \vec{r}} \frac{v_0}{c}$$

and

(6)

$$j_y = i\sigma_0 k_g \frac{v_0}{c} e^{i\vec{k}_g \cdot \vec{r}}$$

35

1 where the electron is assumed to be moving in the x-
 direction at velocity v_0 , k_g is assumed to be oriented
 in this direction, and y is in the direction perpendicular
 to the grating.

5 For an observation point in the x-y plane defined
 by the electron velocity and the perpendicular to the
 grating at an angle θ above the grating, this current
 density gives:

$$10 \quad d\epsilon_\omega = \frac{k^2 e^2 v_0^2 T}{8\pi^3 c^3} e^{-2\Delta k l} g(\omega + \Delta k \cdot v_0) \quad (7)$$

$$\{b^2(\Delta k)^2 \sin^2 \theta + \cos^2 \theta\} d\Omega d\omega$$

where

$$\Delta k = k_g - k \cos \theta \quad (8)$$

15

and T is the total time the electron interacts with the
 grating.

FIG. 2 compares this simple expression with the
 numerical results obtained by the Green's function
 20 formulations. The angular distribution of intensity
 compares well. In FIG. 2, the solid curve represents
 the simple model of Equation 7 and the dashed curve
 depicts the results of the Green's function formulation.

25 2. Spontaneous Radiation from Electrons Moving Through the Salisbury Troughs Formed by Electrons Reflecting from the Grating.

Following his early experiments, Salisbury proposed
 that the electrons reflected from the grating formed
 30 sheets of space-charge having the same periodicity as
 the grating. W. W. Salisbury, U.S. Patent No. 2,634,372
 (1949); W. W. Salisbury, J. Opt. Soc. Am., 60, 1279
 (1970). Other electrons passing through these sheets
 of space-charge would then be alternately accelerated

35

1 and decelerated by the electrostatic forces between
them and the electrons comprising the space-charge
sheets. Since the space-charge would occupy the region
even far from the grating, this would permit distant
5 electrons to radiate as well as electrons that are
close to the grating. Thus, in this hypothesis, in
addition to the surface currents responsible for the
radiation in the Smith-Purcell-type experiment (where
the electrons do not scatter from the grating), bulk
10 currents in the space above the grating can also
contribute.

To describe the characteristics of this "Salisbury"
radiation, a simple model is considered in which
electrons scatter off the surface at an angle θ , creating
15 potential troughs through which the unscattered electrons
then move. This is illustrated in FIG. 3.

For a grating of spatial period a , the troughs
will have a period a in the x -direction and a period
 $a/\tan\theta$ in the y -direction, where coordinate axes have
20 chosen so that x lies parallel to the grating along the
direction of the unscattered electron velocity, and the
 y -direction is perpendicular to this grating, and the y -
direction is perpendicular to this grating. The basic
features of the radiation to determine in this model
25 can be calculated from a crude approximation by which
the electrostatic potential ϕ_G of the troughs is
given by only the lowest term in its harmonic expansion:

$$\phi_G = \phi_1 \exp[ik_{G_x}x + ik_{G_y}y] \quad (9)$$

30

where

$$k_{G_x} = 2\pi/a, \quad k_{G_y} = 2\pi/a \tan\theta \quad (10)$$

35

1 Electrons moving through this potential will
radiate, with the energy $d\epsilon_\omega$ radiated into the element
of solid angle $d\Omega$ in the k -direction, in the form of
waves with frequencies in the angular frequency interval
5 $d\omega$. The incoherent portion $d\epsilon_{inc}$ of the radiation
arises from the uncorrelated motion of the electrons.
By similar analysis which led to Equation 7, it can be
shown that:

$$10 \quad \frac{d\epsilon_{inc}}{d\Omega d\omega} = \frac{Ne^2 \phi_l^2 k_{Gx} T}{\pi c^3 m} S(\theta) \delta\left(\omega + \frac{k_{Gx} v_o}{1 - \frac{v_o}{c} \cos \theta}\right) \quad (11)$$

with

$$15 \quad S(\theta) = \frac{S(\theta)}{1 - \frac{v_o}{c} \cos \theta} = \frac{1}{(1 - \frac{v_o}{c} \cos \theta)^2} \left[\sin \theta - \frac{k_{Gy}}{k_{Gx}} \left(\cos \theta - \frac{v_o}{c} \right) \right]^2 \quad (12)$$

20 For $k_{Gy} = 0$, $S(\theta)$ is peaked in the forward quadrant at:

$$\theta = \cos^{-1} \left[\frac{c}{Gv_o} \left\{ -2 \pm (4 + 60 \left(\frac{v_o}{c} \right)^2)^{1/2} \right\} \right] \quad (13)$$

25 At the other extreme, when $k_{Gx} = 0$, $S(\theta)$ is peaked at:

$$\theta = \cos^{-1} \left[\frac{5}{3} \left(\frac{v_o}{c} \right) - \frac{2}{3} \left(\frac{c}{v_o} \right) \right] \quad (14)$$

and has a zero at:

$$30 \quad \theta = \cos^{-1} \left(\frac{v_o}{c} \right) \quad (15)$$

1 3. Spontaneous Radiation Conclusions.

The spontaneous radiation due to surface currents is much greater in intensity than the spontaneous radiation arising from acceleration of the electrons in the potential troughs created by the scattered electrons. This is because the amplitude of the perturbations in the surface currents due to the grating is much larger than the perturbations in the electron trajectory due to the potential troughs. The former is of the order of b , the grating amplitude (equal to one-half the grating depth), while the latter is of the order of $e\delta\psi/mv_0\omega$ where $\delta\psi$ is the potential due to the troughs, m is the electron mass, and ω is of the order of $k_g v_0$. From Poisson's equation, $\delta\psi \sim k_g^{-2} m_s e$ where m_s is the density of scattered electrons. Thus, since the spontaneous radiation intensity is proportional to the square of the perturbation amplitude, the ratio of the surface current radiation to the trough radiation is of the order of magnitude given in Equation 16.

$$\frac{\text{Surface current radiation}}{\text{Trough Radiation}} = 0 \left[\left(\frac{b k_g^3 m v_0^2}{m_s e^2} \right)^2 \right] \quad (16)$$

For typical parameters in Salisbury's early experiments, $b = 10^{-14}$ cm, $k_g = 10^4$ cm⁻¹, $m v_0^2 = 2 \times 10^{-7}$ ergs, $n_s = 10^8$ cm⁻³, this ratio is $0(10^{24})$. Accordingly, if the periodic space-charge structure due to the scattered electrons is to have any effect on the total spontaneous radiation, it must be through amplification of the spontaneous radiation from the induced surface currents.

B. Coherent (Stimulated) Radiation

1. Amplification of Radiation Moving Through the Periodic Space Charge Structure Formed by Electrons Reflecting from Grating

In order for an electron beam to amplify an electromagnetic wave, the electrons must interact resonantly with the wave, i.e., the wave must have a component with a phase velocity whose projection in the direction of the electron motion is equal to or less than the electron velocity. The periodic space charge created by the electrons reflecting from the grating makes possible this situation. Thus, an electromagnetic wave which in the absence of this periodic space-charge structure would have the dependence $\vec{E} = (\vec{E}_{kx}\vec{i}_x + \vec{E}_{ky}\vec{i}_y) e^{i(\omega t - \vec{k} \cdot \vec{r})}$ will in the presence of the periodic

structure have the form
$$e^{i\omega t} \sum_{n=-\infty}^{n=\infty} \vec{e}_1(\vec{k} + n\vec{k}_g) \cdot \vec{r} \alpha_n.$$

The magnitude of the spatial sideband amplitudes $|\alpha_n|$ is determined by solving Maxwell's equations with the equations of motion for the electrons.

The phase velocity of the n th sideband is $\omega/|k + nk_g|$ and can be equal to or even less than an electron velocity. This permits resonant transfer of energy from the electrons to the waves, resulting in considerable amplification of the radiation. As an example, it is assumed that the unperturbed electron distribution is described by the distribution function:

$$f_0 = n_0 \left(\frac{m}{2\pi kT} \right)^{3/2} \frac{\alpha_1}{\pi} \exp \left[-\frac{m}{2kT} (v_x - v_0)^2 - \alpha_1 (v_y^2 + v_z^2) + \frac{e}{2} (1 + \cos(k_{gx}x + K_{gy}y)) n_0 \left(\frac{m}{2\pi kT} \right)^{1/2} \frac{\alpha_1}{\pi} \exp \left[\frac{-m}{2kT} (v_x - v_0)^2 - \alpha_1 (v_y^2 + v_z^2) \right] \right] \quad (17)$$

1 This describes a group of electrons of temperature
 T and average density n_0 drifting with velocity v_0 in
 the y-direction. Boltzmann's constant is indicated by
 k, and the presence of electrons scattered from the
 5 periodic grating surface is described by the
 $\xi \cos(k_{Gx}x + k_{Gy}y)$ term.

Solution of Maxwell's equation with the equations
 of motion leads to the result that the energy transferred
 per second from the electrons in a unit volume to the
 10 radiation field is $|A+B+C+D|$, where:

$$\begin{aligned}
 A &= \frac{z1}{k_x^+} [E_{kx}^+]^2 (v_0 + \delta v) \exp\left[-\frac{m}{2kT}(\delta v)^2\right] + \\
 15 \quad &\frac{z2}{(k_x^+)^2} \left[\frac{1}{(k_x^+)^2} (k_x^+ E_{ky}^+ - k_y^+ E_{kx}^+) E_{ky}^+ - \frac{1}{(k_x^+)^3} (k_x^+ E_{ky}^+ - k_y^+ E_{kx}^+)^2 + \right. \\
 &\quad \left. \frac{k_y^+}{4(k_x^+)^2} E_{ky}^+ E_{kx}^+ - \frac{k_y^+}{2(k_x^+)^3} (k_x^+ E_{ky}^+ - k_y^+ E_{kx}^+) E_{kx}^+ \right] \exp\left[-\frac{m}{2kT}(\delta v)^2\right] \\
 20 \quad B &= \frac{z2}{k_x^+} \left[E_{ky}^+ r - \frac{1}{k_x^+} (k_x^+ E_{kx}^+ - k_y^+ E_{ky}^+)^2 \right] \exp\left[-\frac{m}{2kT}(\delta v)^2\right] \\
 C &= \frac{z3}{k_x^+} [E_{kx}^+ E_{kx}^+ (v_0 + \delta v) \delta v] \exp\left[-\frac{m}{2kT}(\delta v)^2\right] + \\
 25 \quad &\frac{z2}{4} \left[\frac{1}{(k_x^+)^2} (k_x^+ E_{ky}^+ - k_y^+ E_{kx}^+) E_{ky}^+ - \frac{1}{(k_x^+)^3} (k_x^+ E_{ky}^+ - k_y^+ E_{kx}^+) \right. \\
 &\quad \text{times } (k_x^+ E_{kx}^+ - k_y^+ E_{kx}^+) + \frac{k_y^+}{4(k_x^+)^2} E_{ky}^+ E_{kx}^+ - \frac{k_y^+}{2(k_x^+)^3} (k_x^+ E_{ky}^+ - k_y^+ E_{kx}^+) E_{kx}^+ \\
 30 \quad &\text{times } \exp\left[-\frac{m}{2kT}(\delta v)^2\right] \\
 D &= \frac{z2}{4k_x^+} \left[\left(E_{ky}^+ - \frac{1}{k_x^+} (k_x^+ E_{ky}^+ - k_y^+ E_{kx}^+) \right) \left(E_{ky}^+ - \frac{1}{k_x^+} (k_x^+ E_{ky}^+ - k_y^+ E_{kx}^+) \right) \right. \\
 35 \quad &\text{times } \exp\left[-\frac{m}{2kT}(\delta v)^2\right]
 \end{aligned}$$

(18)

$$z_1 = \frac{e^2}{kT} \left(1 + \frac{\xi}{2}\right) n_0 \sqrt{\frac{m}{2\pi kT}}$$

$$z_2 = \frac{e^2}{m} n_0 \left(1 + \frac{\xi}{2}\right) \sqrt{\frac{m}{2\pi kT}}$$

$$z_3 = \frac{e^2}{kT} \frac{\xi}{4} n_0 \sqrt{\frac{m}{2\pi kT}}$$

$$\text{and } k_x^+ = k_x + k_{gx}, \quad k_y^+ = (k_y + k_{gy}).$$

In the above it has been assumed that $\omega = (k_x + k_{gx})v_0 + \delta_v(k_x + k_{gx})$ where δ_v is some fraction 0(1) of the thermal velocity. The above dispersion condition plus the radiation condition $\omega = kc$ implies that:

$$k = \frac{2\pi}{a[\beta^{-1} - \cos\theta]},$$

where a is the grating spacing, and:

$$\beta = \frac{v_0 + \delta_v}{c} \quad (19)$$

FIGS. 4a, 4b, 4c show normalized plots of energy transfer from electrons to the radiation field for representative parameters and for different values of electron density, n_0 . In the figures, the following list of parameters is used, with:

$$\begin{aligned} a &= 10^{-4} \text{ cm} \\ k_{gx} &= 2 \text{ f/a} \\ k_{gy} &= -10 k_{gx} \\ v_0 &= 2 \times 10^{10} \text{ cm/sec} \\ T &= 100^\circ \text{K} \\ n_0 &= 10^8 \text{ particles/cm}^3 \text{ (FIG. 4a)} \\ &= 10^{10} \text{ particles/cm}^3 \text{ (FIG. 4b)} \\ &= 10^{12} \text{ particles/cm}^3 \text{ (FIG. 4c)} \end{aligned}$$

1 It is therefore apparent from the foregoing that
coherent radiation can be obtained even in the absence
of a cavity when electrons are reflected from a grating.
The condition for the coherent radiation to dominate
5 the incoherent radiation is that the spontaneous
radiation from the induced surface currents must
experience an (inverse Landau damping) amplification
gain greater than unity on moving through the periodic
space-charge structure above the grating. An amplification
10 gain greater than unity occurs when the total average
energy transfer from the electrons to the radiation
field is greater than the energy radiated by the induced
surface currents (given in Equation 7). The gain G is
equal to the ratio I/I_{input} , where:

15

$$I = \int dv^3 [A+B+C+D]/r.$$

I_{input} is given by Equation 7 and is the radiation
intensity from the induced surface currents.

20 The amplification gain greater than unity occurs
for reasonable parameter values when the electron beam
is thick enough, dense enough, and well collimated
enough to give a well defined periodic space-charge
structure on reflection. By way of example only, the
25 following are presently considered reasonable parameter
values: .1 to 1 milliradian beam divergence, beam
densities on the order of 10^8 particles/cm², particle
energies on the order of 100 kV, and grating spacings
on the order of 10,000 Angstroms. These values are
30 exemplary only; other values are also reasonable and
attainable.

 If the space-charge structure is not well-defined,
there would not be an effective mechanism to impart
energy from the electron beam to the radiation generated
35 by the grating surface currents.

1 2. Coherent Radiation from Collective Effects for
 an Electron Beam Moving Through the Periodic
 Space-charge Structure Formed by Electrons
 Reflecting from Grating

5 Coherent radiation can also arise from the
 correlated motion of the electrons. Equation 20 gives
 the radiation vector potential as an integral over \vec{j}_ω ,
 the ω -frequency fourier component of the current density.

10
$$\vec{A}_\omega = \frac{e i k R_0}{c R_0} \int \vec{j}_\omega e^{-i \vec{k} \cdot \vec{r}} d^3 r \quad (20)$$

 Equation 20 shows that if \vec{j}_ω has a spatial
 variation of the form $e^{i \vec{k} \cdot \vec{r}}$ with $\vec{k} = \omega/c$, then the
 integrand does not have a spatial oscillation and,
 15 therefore, does not tend to be self-cancelling on
 integration. Accordingly, a current density with this
 form of spatial variation can make a very large
 contribution to the radiation field.

 To determine if electrons moving through the
 20 potential troughs can give rise to a large microscopic
 current variation of the form $e^{i \vec{k} \cdot \vec{r}}$, the Vlasov
 equation for an electron distribution function $f(\vec{r}, \vec{v}, t)$
 can be considered. Here $f(\vec{r}, \vec{v}, t)$ denotes the number
 of electrons in spatial volume $d^3 r$ at position r and the
 25 velocity interval $d^3 v$ at velocity v , and satisfies the
 equation:

$$\frac{\delta f}{\delta t} + \vec{v} \cdot \nabla f - \frac{e}{m_0} \Delta \psi \cdot \nabla_v f = 0 \quad (21)$$

30 From the solution of Equation 21 along with
 Poisson's equation for the electrostatic potential ψ :

$$\Delta^2 \psi = 4 \pi n e \quad (22)$$

1 it may be demonstrated that electrons moving through
 the stationary potential troughs ϕ_G of Equation 9 can
 give rise to spatial variations in the current density
 $j_\omega(r)$ of the form $e^{i\vec{k} \cdot \vec{r}}$, $|\vec{k}| = \omega/c$. This occurs
 5 when these equations are solved through second order in
 ϕ_G .

Solution of these equations give current densities
 which have spatial and time variations of the form:

- 10 (a) $e^{-i(\omega_s t - k_{sx}x - k_{sy}y)}$
 (b) $e^{i(k_{Gx}x + k_{Gy}y)}$
 (c) $e^{-i(\omega_s t - (k_{sx} \pm k_{Gx})x - (k_{sy} \pm k_{Gy})y)}$

Thus, j_ω varies as $e^{-i(\omega \vec{t} \cdot \vec{k} \cdot \vec{r})}$ when:

15 $\omega = \omega_s$ (23a)

$k_x = k_{sx} \pm k_{Gx}$ (23b)

$k_y = k_{sy} \pm k_{Gy}$ (23c)

20 this component will give rise to coherent radiation.

To determine what frequencies ω_s are likely to
 be excited in the beam of interaction with the troughs,
 the equation for the density of the beam in the frame x
 moving with the beam is considered.

25 $\frac{\partial^2 n}{\partial t^2} + \omega_p^2 n = -\omega_p^2 n_a$ (24)

In this equation, n_a denotes the density of the electrons
 comprising the troughs through which the unscattered
 30 electrons of density n move. To determine what
 frequencies are likely to be excited, the Green's
 function solution for $n = \delta(x + v_0 t)$ is considered, i.e.,
 for a delta-function trough which is fixed in the frame
 of the grating. The solution to Equation 24 for this
 35 n_a is:

1
$$n(x,t) = -\omega_p \sin\left[\frac{\omega_p}{v_0}(x + v_0 t)\right] \quad (25)$$

5 Thus, the frequency excited is ω_p . A sum over many δ functions for n_a gives the same frequency of excitation.

As a result, it is apparent that collective effects can be used to enhance the intensity of coherent radiation from an electron beam scattering off a diffraction grating. This will occur when the plasma frequency ω_p of the beam is comparable to the radiation frequency. The latter is of the order of v_0/a , where v_0 is the electron velocity and a is the grating spacing. This is presently a practical condition for mm-wave frequencies.

C. Additional Embodiments

1. Other Techniques for Creating the Space-charge Structure

20 From the foregoing, additional ways may be seen to improve the performance of a radiation source based on the interaction of electrons with a conductive grating. Since the periodic space-charge structure above the grating has been seen to play an important role in giving high intensity radiation, other means of creating this structure can be considered besides scattering electrons from the grating. One way, for instance, to have an accelerating grid structure oriented so as to inject sheets of electrons transverse to the radiating electron beam. This is illustrated in FIG. 5a. Accordingly, the periodic space-charge structure may be created by means other than scattering an electron beam from a grating, e.g., by using a periodic Pierce

1 electrode structure to create sheets of charged particles
transverse to beam as well as to create induced surface
current. Periodic Pierce electrode structures are well
known, e.g., "ICF Neutralized Light Ion Beam Studies
5 with Ballistic Focusing, Time Compression and Low
Temperature Source", D. B. Chang and W. Salisbury, 1980
IEEE International Conference on Plasma Science, May 19-
21, 1980. In this embodiment, for example, a periodic
Pierce electron gun may be employed which comprises an
10 electron emitter, a low voltage, space-charge limited,
extraction and acceleration gap, and a high voltage,
source limited acceleration and focusing gap. This
structure is illustrated in FIG. 5b, where the extraction
and acceleration gap 110 is between the electron emitter
15 105 and extraction grid 115. The high voltage acceleration
and focusing gap 120 is disposed between the extraction
grid and the acceleration grid 125. The beam is
preferably uniform in one dimension with a 1 mm periodic
Pierce electron gun structure is analogous to the
20 structure of periodic ion injectors designed for inertial
confinement fusion applications.

2. Cavity Devices

Another way to increase the radiation intensity
25 is to place the beam-grating structure inside a cavity.
An exemplary structure is shown in FIG. 6. An essential
difference between this resulting cavity device and
existing cavity devices such as the above-noted Orotron
and Ledatron devices is that the periodic space-charge
30 structure extending far above the grating would allow
electrons distant from the grating to interact resonantly
with the cavity field instead of just those electrons
within a grating spacing of the grating. This results

1 from the fact that, in these known devices, the electron
beam does not impinge on the grating. With this
technique, it is expected that higher electron densities
and more clearly defined sheets of electrons with more
5 sharply defined boundaries will be obtained. The
electron sheets need not be perpendicular to the
electrode structure.

For these cavity devices several ways of increasing
the intensity are apparent. An illustrative embodiment
10 of a radiation source employing a superconducting cavity
is shown in FIG. 7. The grating 200 and cavity 210 are
disposed within evacuated helium dewar 220 to reduce
the temperature of the cavity 210 to below 20°k. The
cavity 210 is fabricated from a superconductor material,
15 such as Nb₃Sn; alternatively, a thin film of supercon-
ductive material may be formed on the grating side of
a substrate. The electron beam generator (not shown)
need not be disposed within dewar 220, but rather may
be disposed to communicate the electron beam 230 through
20 an opening 225 so as to impinge on the grating at a
glancing angle. The resulting radiation 250 may be
emitted from the dewar through window port 240.

The superconductive material has a near total
loss of resistance at a critical temperature that is
25 characteristic of each material. Thus, as the cavity
material is cooled below its critical temperature, the
cavity mirror becomes less lossy, enhancing the intensity
of the emitted radiation.

With the Q of the cavity much larger than that of
30 present devices, this will permit the resonant fields
to increase so that more energy can be transferred
between the beam electrons and the field.

1 The cavity may also be constructed so that the
reflecting faces capture the radiation at those angles
for which maximum intensity occurs. This may require a
cavity with three reflectors (including the grating),
5 for instance, rather than two. An illustrative structure
is shown in FIG. 8.

Referring now to FIG. 9, a radiation source
employing a planar mirror is illustrated. In this
embodiment a planar mirror 300 is supported above the
10 grating 310, with the mirror surface 305 facing the
grating. The electron beam 320 is passed between the
grating and mirror surface. The mirror may be placed
very close to the grating so that the generated radiation
325 can be amplified in the slow wave space-charge
15 sheets through a great number of bounces between the
mirror and the grating.

3. Grating Blaze Angle

Another way to increase the intensity is to orient
20 the blaze angle of the grating so as to enhance either
a cavity mode or the radiation in the direction of
maximum intensity. It may also be of advantage to make
the grating depth equal to a quarter wavelength in
order to force the radiation intensity to be larger in
25 directions away from the grating.

To determine the direction of the maximum intensity,
the magnitude of emitted radiation from induced surface
currents must be considered as well as the radiation
amplification in the space-charge sheets. The former
30 factor is calculated by Equation 7; the latter factor
results from the solution of Equation 25. FIGS. 10(a)-(c)
illustrate graphically the determination of the angle
at which maximum intensity occurs. FIG. 10(a) represents

1 the amplitude of the radiation emitted as a result of
induced surface currents as a function of the viewing
angle θ (Equation 7). FIG. 10(b) depicts the amplifi-
cation of radiation passing through the space-charge
5 structure, as a function of the viewing angle θ and
for a particular angular orientation of the space-
charge structure in relation to the grating (Equation 25).
FIG. 10(c) represents the produce of the emission
amplitude (10(a)) and amplification factor (8(b)). The
10 resulting product curve then has an amplitude peak at a
particular observation angle θ_c .

Because the magnitude of the amplification through
the space-charge sheets is dependent on their angular
relationship to the grating, the amplification should
15 be varied as a function of this angle, and the product
of the amplification and emission amplitude recalculated
to optimize the peak. This is illustrated by the three
curves shown in FIG. 10(d), each representing the
product resulting from a particular angular orientation
20 of the space-charge sheets.

Once the angular orientation of the space-charge
sheets and the observation angle has been determined
for which the maximum intensity is obtained, then the
grating blaze angle may be selected so as to result in
25 the space-charge sheets being directed in the angle for
which the maximum intensity is obtained.

4. Multi-frequency Radiation Source

The radiation source described above provides
30 a means of simultaneously giving radiation at several
different wavelengths, with the interesting feature
that there would be a definite correlation between the
phases of the radiation at different wavelengths. This
can be done by using several beams of electrons of

35

1 32fferent energies, since the wavelength emitted by any
electron depends on its velocity according to Equation 1.
Alternatively, a wide electron beam may be employed
which impacts on two or more gratings of different
5 grating spacing widths, exploiting variation of another
parameter of Equation 1. Yet another technique is to
employ two or more gratings of the same grating spacing
but with one or more oriented obliquely with respect to
the beam direction so that the effective grating spacing
10 is narrowed.

5. Modulation

The radiation from the radiation source can also
be modulated, both in frequency and in amplitude. The
15 former can be achieved easily by varying the acceleration
voltage for the electron beam. The latter can be
obtained by deflecting the beam transversely, so that
the number of electrons impacting the grating may be
varied. Transverse deflection can be achieved by
20 applying a small voltage to the grating itself.

6. X-ray Radiation Source

It is of interest to consider the extension of
this technique to x-ray wavelengths, e.g., to construct
25 a compact x-ray laser. This requires a grating with a
small spatial period. Crystals (e.g., Cu, Ni, Si) can
be used for this purpose for spatial periods which are
on the order of Angstroms. Superlattices can be used
for 0(10-100Å) periods. Exemplary structures are shown
30 in FIGS. 11(a) and 11(b), respectively, employing the
crystalline and superlattice structure. As is shown,
the superlattice structure is a semiconductor doped
with impurities (indicated by "x" in FIG. 11(b)). The
periodic space-charge structure can be obtained either

1 by Bragg reflecting electrons from these lattices, or
transmitting charged particles through the lattices to
created sheets of space-charge. Channeling would help
define the sheets in the latter case. For the reflection
5 mode of operation, the beam would have to be very well
collimated in order that the space-charge periodicity
would extend an appreciable distance from the grating.
The surfaces of the crystal or semiconductor need to be
conductive so as to set up the surface currents which
10 create the radiation. The conductivity needs to be
high enough to drain the charge from the grating to
prevent the surface charge from repelling the electron
beam. In the case of the semiconductor, its conductivity
may be sufficient for this purpose.

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7. Broadband Radiation Source

The above embodiments have contemplated that the
electron beam would strike the grating at a grazing
angle, to optimize the number of electrons which are
20 reflected from the grating so as to set up the periodic
space-charge structure. It has been found that if the
electron beam strikes the grating at angles larger than
grazing angles so that a significant number of electrons
are trapped in the grating rather than being reflected,
25 significant broadband noncoherent radiation is generated.
Electrons which are trapped within the grating material
are decelerated, and this change in velocity gives rise
to Bremsstrahlung radiation, a well-known phenomenon.
This radiation is broadband and noncoherent. In fact,
30 this type of radiation can be generated by impacting
the electron beam onto a polished surface. This property
can be exploited to provide an added capability to the
radiation source of the present invention. Thus, in
FIG. 1, the grating may simply be tilted to a significant
35 angle with respect to the incident beam. Significant
broadband radiation will be produced as a result.

1 It is understood that the above-described
embodiments are merely illustrative of the many possible
specific embodiments which can represent principles of
the present invention. Numerous and varied other
5 arrangements can readily be devised in accordance with
these principles by those skilled in the art without
departing from the spirit and scope of the invention.

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CLAIMSWhat is Claimed is:

- 1 1. In a radiation source employing a conductive
grating and electron beam means adapted to direct a beam
of electrons above the grating so as to generate
spontaneous radiation from the interaction of the
5 electron beam and the conductive grating, the improvement
for generating coherent radiation comprising:

 means for providing a periodic space-charge
structure of electrons above the grating such that the
spontaneous radiation passes through said space-charge
10 structure, said means being adapted such that the
spontaneous radiation experiences an amplification gain
greater than unity on passing through the periodic
space-charge structure above the grating.

- 1 2. The improvement of Claim 1 wherein said space-
charge structure means is adapted to provide a well-
defined periodic space-charge structure.

- 1 3. The improvement of Claim 2 wherein said space-
charge structure means comprises means for causing said
electron beam to collide with said grating at a grazing
angle, whereby electrons scattered from said grating
5 structure comprise said periodic space-charge structure.

- 1 4. The improvement of Claim 3 wherein said
electron beam means is adapted to provide a dense,
collimated beam.

1 5. The improvement of Claim 4 wherein said
electron beam means is adapted provide a beam density
of at least 10^8 particles/cm³, with a beam divergence
in the range of .1 to 1 milliradians.

1 6. The invention of Claim 1 wherein said means
for providing a periodic space-charge structure comprises
means for passing sheets of charged particles through
said grating in a transverse relationship with said
5 electron beam.

1 7. The invention of Claim 6 wherein the means
for passing sheets of charged particles through the
grating comprises a periodic Pierce electrode structure.

1 8. The invention of Claim 1 further comprising
means for modulating the amplitude of the radiation.

1 9. The invention of Claim 8 wherein the modulating
means comprises means for impressing a deflection
voltage on the grating.

1 10. The invention of Claim 1 further comprising
means for modulating the frequency of the radiation
from the source.

1 11. The invention of Claim 10 wherein means for
modulating the frequency of the radiation comprises
means for varying the velocity of the electrons comprising
the electron beam.

1 12. The invention of Claim 11 wherein the electron
beam means comprises an acceleration voltage means for
accelerating the electron beam for varying the electron
velocity is adapted to modulate the acceleration voltage
5 on the electrons.

1 13. A source of coherent radiation, comprising:
 conductive grating having a grating spacing a ;
 means for providing a periodic space-charge
structure of electrons above said grating; and
5 electron beam means adapted to direct a beam
of electrons through said periodic space-charge structure,
said means being adapted to provide an electron beam
having a natural plasma frequency comparable to the
radiation frequency.

1 14. The invention of Claim 13 wherein said
radiation frequency is of the order of v_0/a , where v_0
is the electron velocity of the electron beam.

1 15. The invention of Claim 13 wherein said means
for providing a periodic space-charge structure and
said electron beam means are cooperatively arranged
such that said electron beam collides with said grating
5 at a grazing angle, whereby electrons scattered from
said grating structure comprise said periodic space-
charge structure.

1 16. A radiation source, comprising:
 conducting cavity means;
 conductive grating means disposed within the
cavity;
5 means for providing a periodic space-charge
structure of electrons above the grating; and
 electron beam means adapted to direct a beam
of electrons through said periodic space-charge structure.

1 17. The radiation source of Claim 16 wherein the
cavity means comprises a superconducting material, and
the radiation source further comprises cooling means
for cooling the cavity, whereby the Q of the cavity is
5 increased to allow increased energy transfer between
the beam electrons and the field.

1 18. The radiation source of Claim 16 wherein the
cavity comprises reflecting faces adapted to capture
the radiation at preselected orientations.

1 19. The radiation source of Claim 18 wherein the
preselected orientations are those which provide maximum
radiation intensity.

1 20. The radiation source of Claim 16 wherein said
cavity comprises a planar mirror surface disposed above
said grating surface, and the electron beam is passed
between the grating and the mirror surface, whereby the
5 spontaneous radiation is repetitively reflected off the
mirror surface back through the space-charge structure.

1 21. In a radiation source employing a conductive
grating and electron beam means adapted to direct a
beam of electrons above the grating so as to generate
spontaneous radiation from the interaction of the
5 electron beam and the conductive grating, the improvement
wherein:

 the conductive grating comprises a crystal
having a reflective surface, wherein the spatial spacing
of the grating is on the order of Angstroms, and the
10 spontaneous radiation comprises x-ray wavelength radiation.

1 22. The invention of Claim 21 wherein said electron
beam is adapted to collide with the reflective surface
of the crystal at a grazing angle, whereby the electrons
scattered from said surface comprise a periodic space-
5 charge structure above the crystal surface.

1 23. The invention of Claim 21 further comprising
a means adapted to pass charged particles through the
crystal so as to create periodic sheets of charged
particles above said reflective surface.

1 24. The invention of Claim 21 wherein said crystal
material comprises one of the group of Cu, Ni or Si.

1 25. In a radiation source employing a conductive
grating and electron beam means adapted to direct a
beam of electrons above the grating so as to generate
spontaneous radiation from the interaction of the
5 electron beam and the conductive grating, the improvement
wherein:
 the conductive grating comprises a superlattice
structure, comprising a reflective surface, wherein the
spatial spacing of the grating is on the order of ten
10 to one hundred Angstroms, and the spontaneous radiation
comprises x-ray wavelength radiation.

1 26. The invention of Claim 25 wherein said electron
beam is adapted to collide with the reflective surface
of the superlattice at a grazing angle, whereby electrons
scattered from said surface comprise a periodic space-
5 charge structure above the crystal surface.

1 27. The invention of Claim 25 further comprising
a means adapted to pass charged particles through the
crystal so as to create periodic sheets of charged
particles above reflective surface.

1 28. A radiation source, comprising:

 a conductive grating whose elements are
characterized by a predetermined blaze angle and a
grating space a;

5 electron beam means adapted to direct a beam
of electrons above said grating, so that said electron
beam collides with said grating at a grazing angle,
whereby electrons reflected from the grating comprise a
periodic space-charge structure of electrons above the
10 grating; and

 wherein the grating blaze angle and the
electron beam means are cooperatively arranged to
enhance the intensity of radiation in a predetermined
direction.

1 29. The radiation source of Claim 18 wherein said
predetermined direction is dependent upon the magnitude
of emission resulting from induced surface currents on
said grating and the orientation of the space-charge
5 structure in relation to the grating.

1 30. The radiation source of Claim 29 wherein the
blaze angle of the grating is oriented so as to orient
the space-charge structure in a predetermined relationship
to maximize the intensity in such predetermined direction.

1 31. A tunable radiation source adapted to
selectively generate broadband incoherent radiation and
coherent radiation over a broad frequency range,
comprising:

5 a conductive grating;
 an electron beam generator adapted to generate
a high energy electron beam;

means for directing the electron beam over
said grating so as to collide with said grating, said
10 means adapted to selectively determine the angle at
which said electron beam collides with said grating;
means for selectively providing a well-defined
space-charge structure above said grating when said
directing means causes the electron beam to collide
15 with the grating at a grazing angle; and
whereby coherent spontaneous radiation is
generated when the beam collides with the grating at a
grazing angle, and Bremsstrahlung radiation is generated
when the collision angle is direct enough that a
20 substantial number of the electrons are absorbed into
the grating.

1 32. A radiation source, comprising:
conductive grating means having a grating
element spacing;
means for providing a periodic space-charge
5 structure of electrons above said grating;
electron beam means adapted to direct a
plurality of beams of electrons of different electron
energies through said periodic space-charge structure,
whereby spontaneous radiation of different wavelengths
10 is generated from the interaction of the electron beams
and the grating means, and whereby the wavelengths of
the radiation are dependent on the electron energies
and the grating spacing.

1 33. The radiation source of Claim 32 wherein said
means for providing a periodic space-charge structure
above said grating is adapted such that the spontaneous
radiation experiences an amplification gain greater
5 than unity on passing through the periodic space-charge
structure above the grating, whereby coherent spontaneous
radiation is generated.

1 34. The radiation source of Claim 32 wherein said
means for providing a space-charge structure comprises
means for causing at least one of said electron beams
to collide with said grating at a grazing angle, whereby
5 electrons scattered from said grating means comprise
said space-charge structure.

1 35. A radiation source, comprising:
 conductive grating means comprising a plurality
of grating elements having a first effective grating
spacing in a first region and a second effective grating
5 element spacing in a second region;
 means for providing a periodic space-charge
structure of electrons above said grating means;
 electron beam means adapted to direct a beam
of electrons through said periodic space-charge structure;
10 and
 whereby spontaneous radiation of two different
wavelengths is generated from the interaction of the
electron beam and the two regions of the grating means,
and whereby the radiation wavelengths are dependent on
15 the electron energy and the grating element spacings.

1 36. The radiation source of Claim 35 wherein said
means for providing a periodic space-charge structure
above said grating is adapted such that the spontaneous
radiation experiences an amplification gain greater
5 than unity on passing through the periodic space-charge
structure above the grating, whereby coherent spontaneous
radiation is generated.

1 37. The radiation source of Claim 35 wherein said
means for providing a space-charge structure comprises
means for causing said electron beam to collide with
said grating means at a grazing angle, whereby electrons
5 scattered from said grating means comprises said periodic
space-charge structure.

1 38. The radiation source of Claim 35 wherein said
spatial spacing of the gratings in the first grating
region are substantially the same as the spatial grating
spacings in the second region, and wherein the grating
5 elements in the first region and the second region are
disposed so that the angular disposition of the electron
beam with respect to the gratings in the first region
differs from the angular disposition of the electron
beam with respect to the gratings in the second region,
10 whereby the effective grating spacings in the first
region differ from the effective grating spacing in the
second region in the direction of the beam.

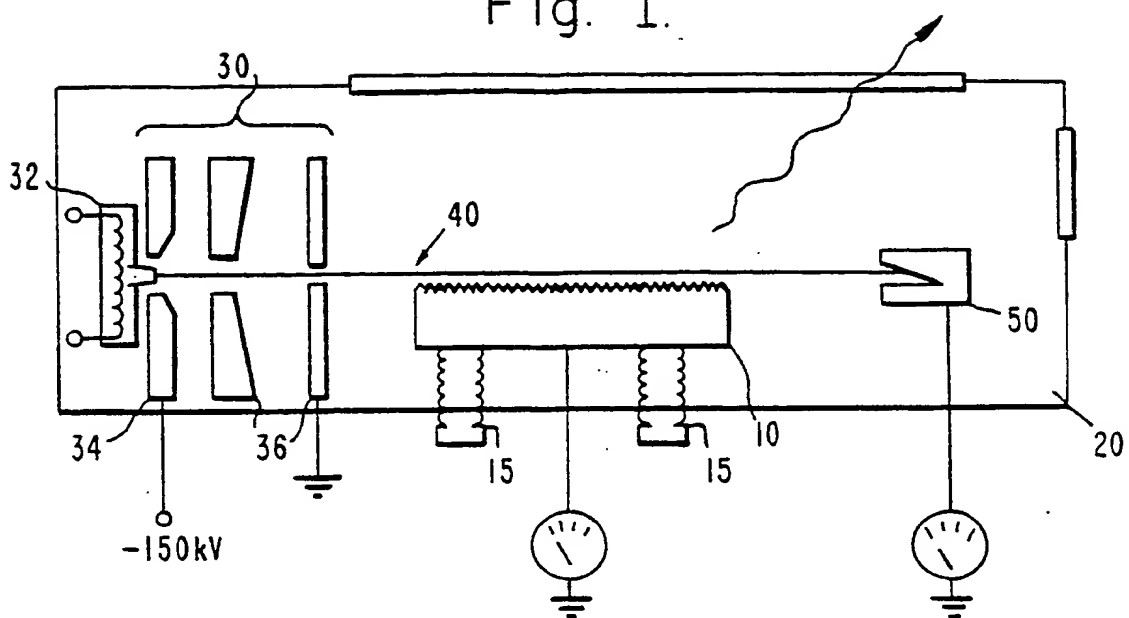
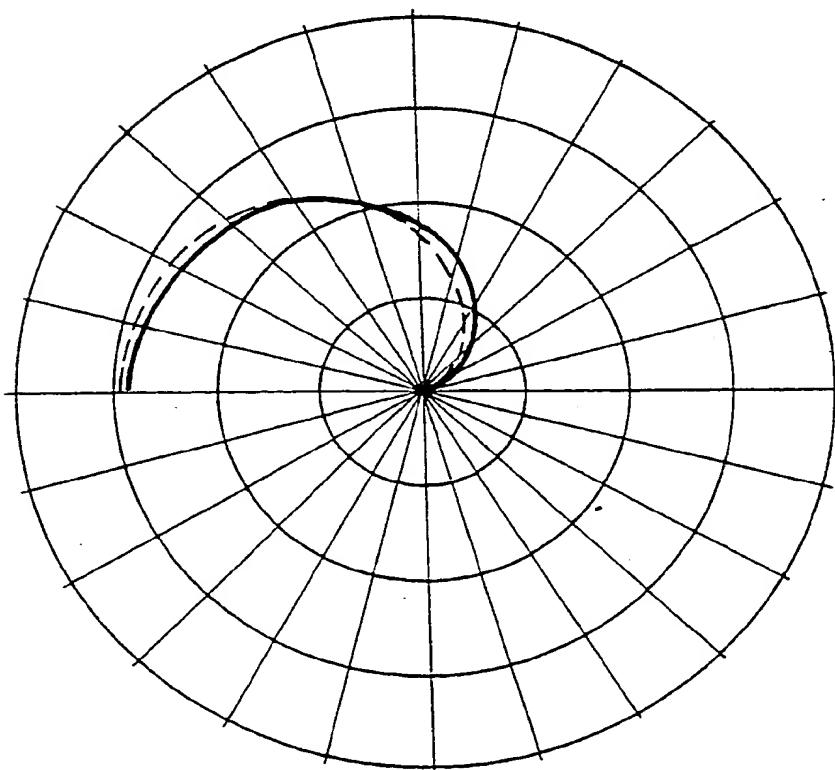
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Fig. 1.

Fig. 2.



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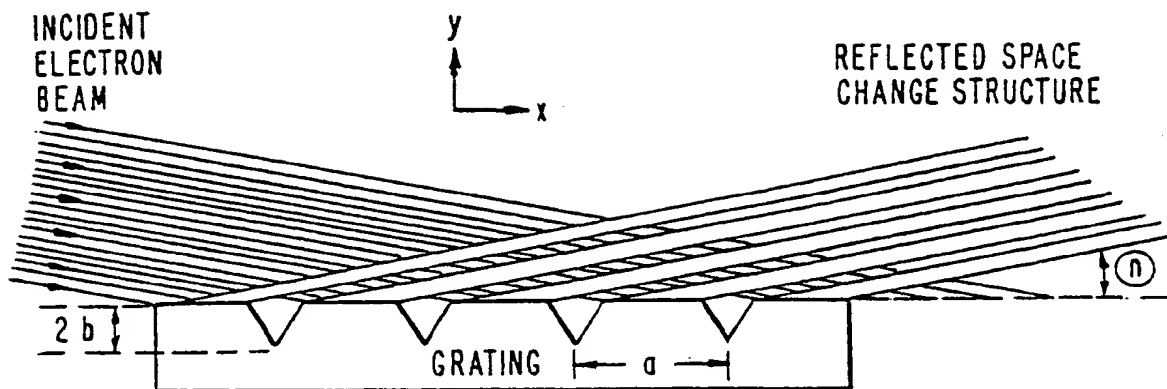


Fig. 3.

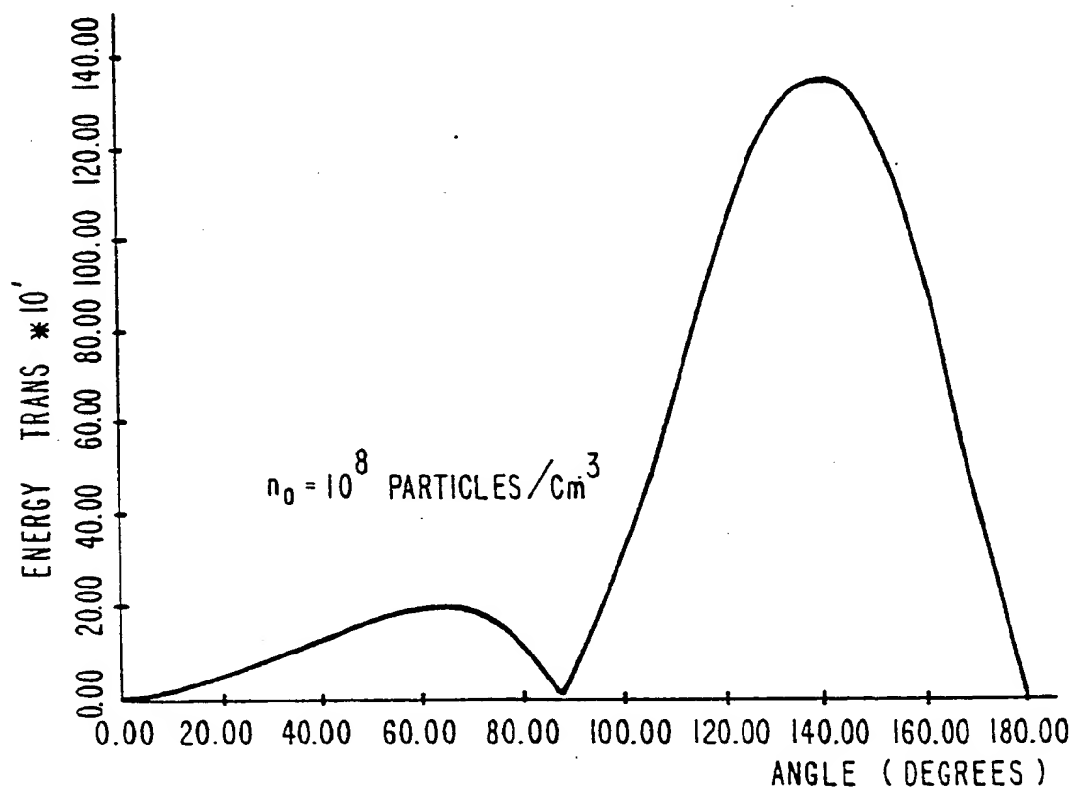
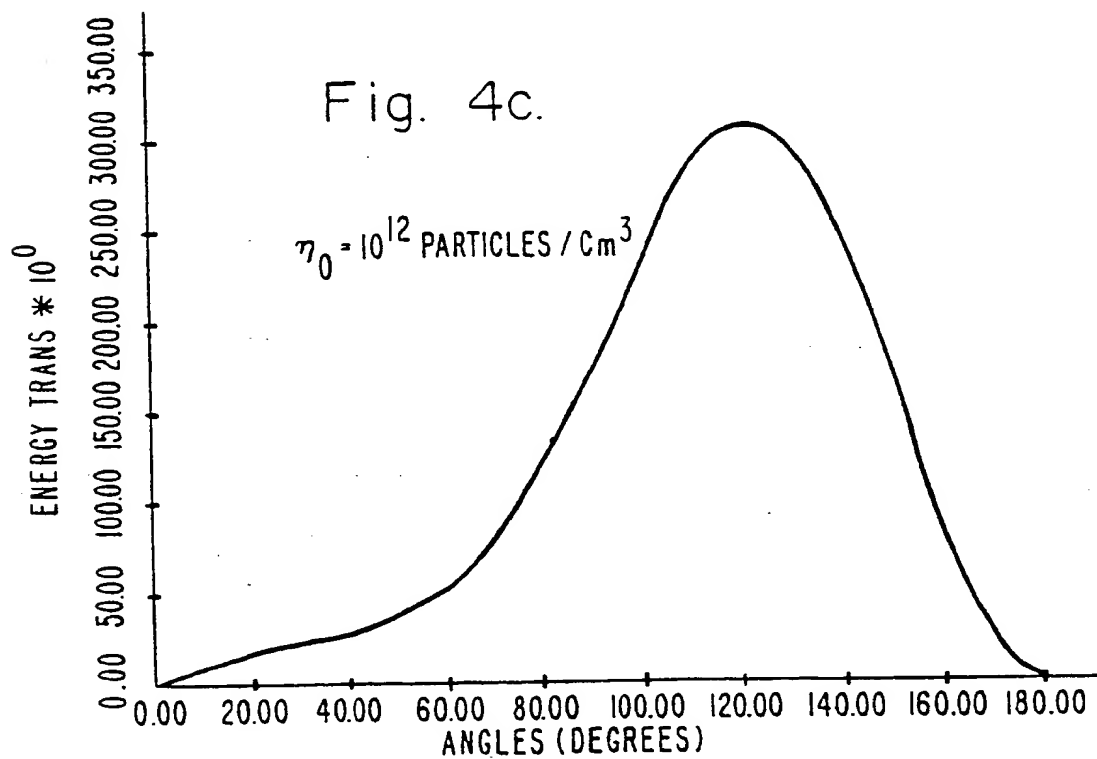
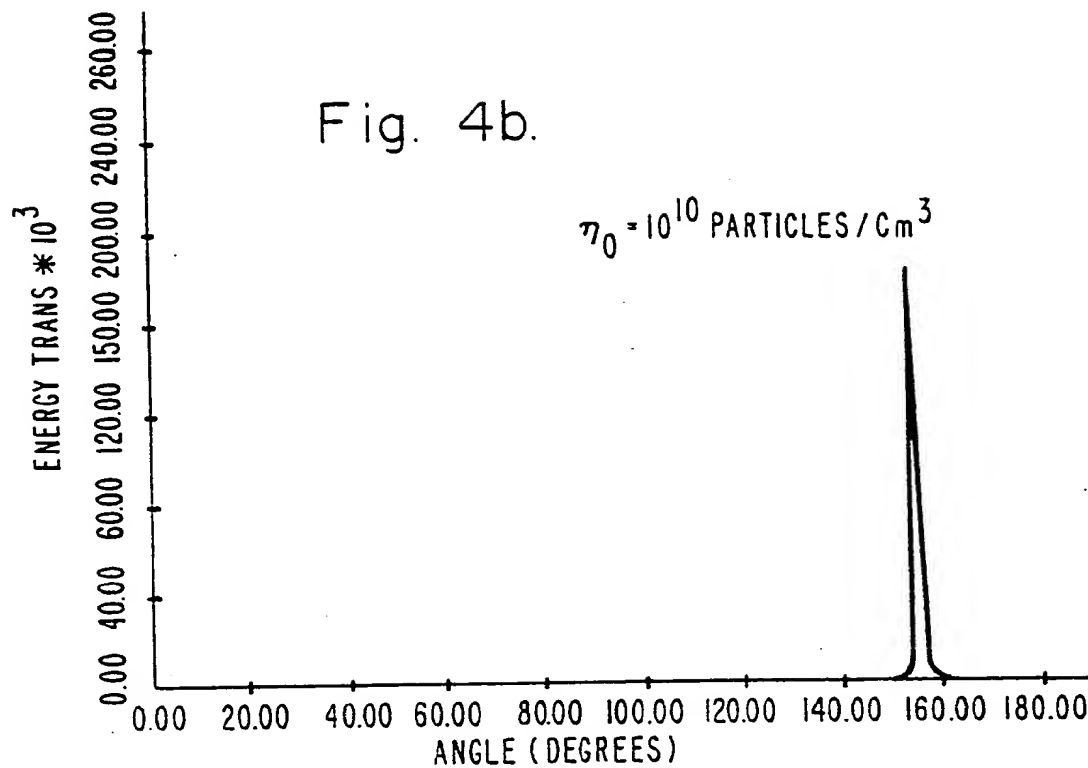


Fig. 4a.

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Fig. 5a.

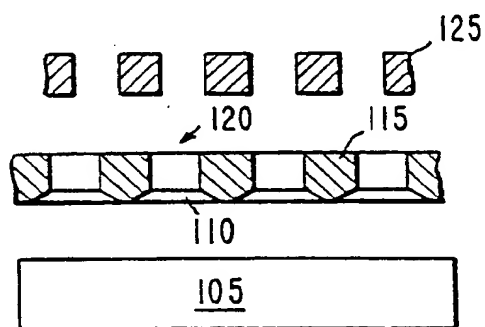
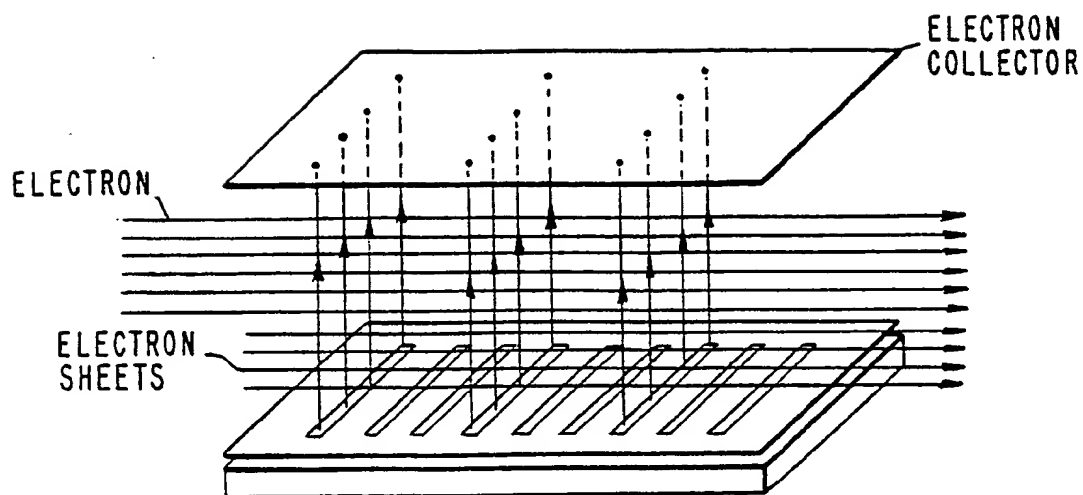


Fig. 5b.

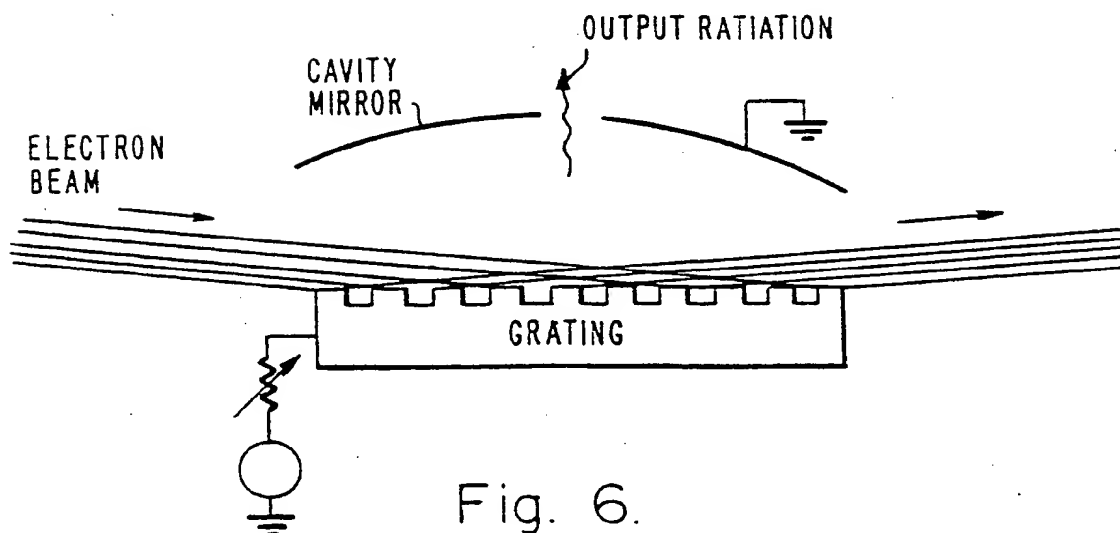


Fig. 6.

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Fig. 7.

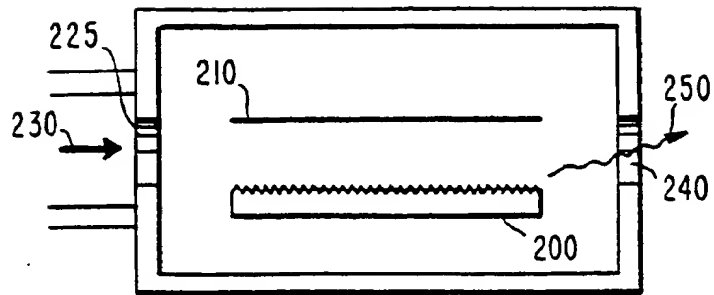


Fig. 8.

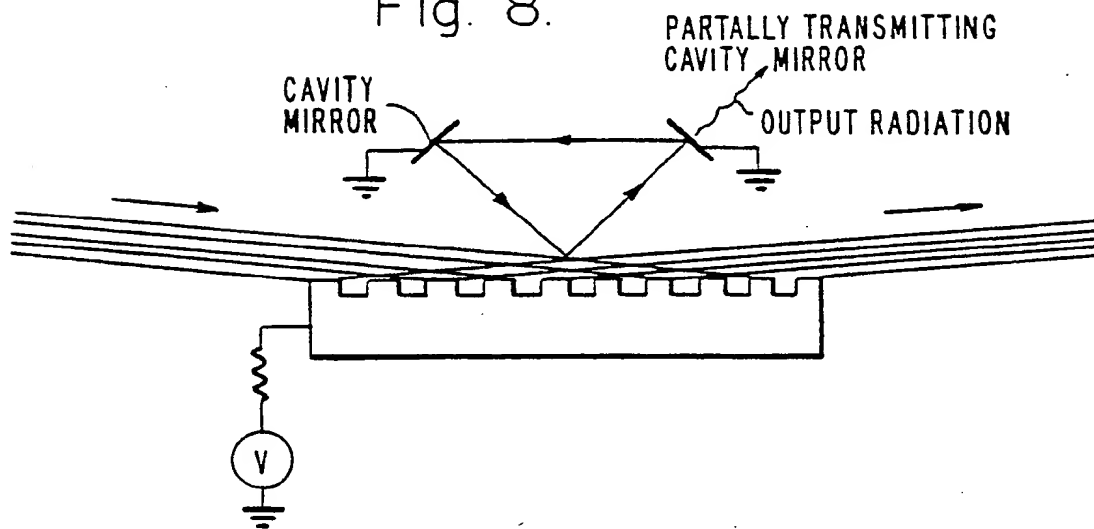
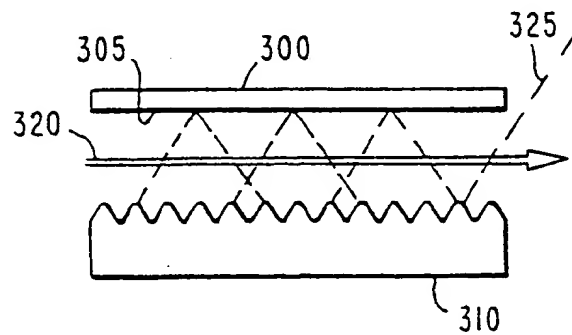


Fig. 9.



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Fig. 10a.



Fig. 10b.



Fig. 10c.

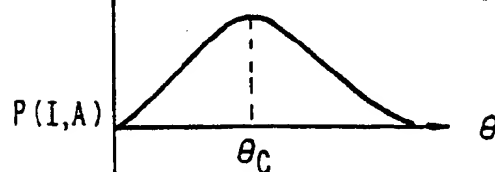


Fig. 10d.

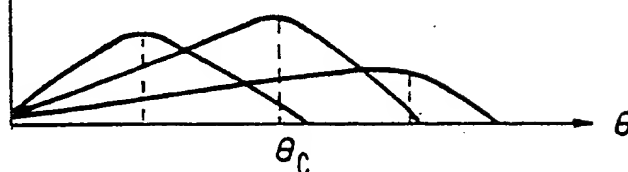
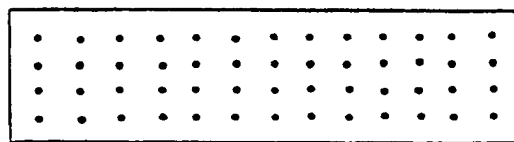
ELECTRON
BEAMPERIODIC
SPACE CHARGE
STRUCTURE

Fig. 11a.



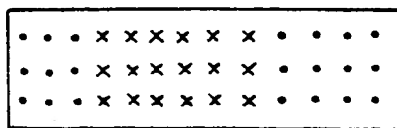
CRYSTAL



ELECTRON BEAM

ELECTRON
BEAMPERIODIC
SPACE CHARGE
STRUCTURE

Fig. 11b.



SUPER LATTICE



INTERNATIONAL SEARCH REPORT

International Application No. **PCT/US 86/01821**

I. CLASSIFICATION OF SUBJECT MATTER (if several classification symbols apply, indicate all) ⁴ According to International Patent Classification (IPC) or to both National Classification and IPC IPC⁴: H 01 S 3/09														
II. FIELDS SEARCHED <div style="text-align: center; border-top: 1px solid black; border-bottom: 1px solid black; margin: 5px 0;">Minimum Documentation Searched ⁷</div> <table style="width: 100%; border-collapse: collapse;"> <tr> <th style="width: 25%; border-bottom: 1px solid black;">Classification System</th> <th style="border-bottom: 1px solid black;">Classification Symbols</th> </tr> <tr> <td style="border-right: 1px solid black; padding: 5px;">IPC⁴</td> <td style="padding: 5px;">H 01 S</td> </tr> </table> <div style="text-align: center; border-top: 1px solid black; border-bottom: 1px solid black; margin: 5px 0;">Documentation Searched other than Minimum Documentation to the Extent that such Documents are Included in the Fields Searched ⁸</div>			Classification System	Classification Symbols	IPC ⁴	H 01 S								
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IPC ⁴	H 01 S													
III. DOCUMENTS CONSIDERED TO BE RELEVANT ⁹ <table style="width: 100%; border-collapse: collapse;"> <tr> <th style="width: 10%; border-bottom: 1px solid black;">Category ⁹</th> <th style="border-bottom: 1px solid black;">Citation of Document, ¹¹ with indication, where appropriate, of the relevant passages ¹²</th> <th style="width: 10%; border-bottom: 1px solid black;">Relevant to Claim No. ¹³</th> </tr> <tr> <td style="text-align: center; vertical-align: top; padding: 5px;">Y</td> <td style="padding: 5px;"> Journal of the Optical Society of America, volume 60, no. 10, October 1970, New York (US) W.W. Salisbury: "Generation of light from free electrons", pages 1279-1284, see page 1279, column 1, lines 24-27; page 1281, line 53 - column 2, line 7; page 1283, column 2, lines 22-35; page 1284, column 1, line 13 to column 2, line 5; figure 5 (cited in the application) </td> <td style="text-align: center; vertical-align: top; padding: 5px;">1-38</td> </tr> <tr> <td style="text-align: center; vertical-align: top; padding: 5px;">Y</td> <td style="padding: 5px;"> IEEE Transactions on Electron Devices, volume ED-29, no. 10, October 1982, New York (US) D.E. Wortman et al.: "Improved OROTRON performance in the 50- to 75-GHz frequency region", pages 1639-1640, see abstract; figure 1 </td> <td style="text-align: center; vertical-align: top; padding: 5px;">1-38</td> </tr> <tr> <td style="text-align: center; vertical-align: top; padding: 5px;">Y</td> <td style="padding: 5px;"> Nuclear Instruments & Methods, volume 204, no. 2/3, January 1983, Amsterdam (NL) </td> <td></td> </tr> </table>			Category ⁹	Citation of Document, ¹¹ with indication, where appropriate, of the relevant passages ¹²	Relevant to Claim No. ¹³	Y	Journal of the Optical Society of America, volume 60, no. 10, October 1970, New York (US) W.W. Salisbury: "Generation of light from free electrons", pages 1279-1284, see page 1279, column 1, lines 24-27; page 1281, line 53 - column 2, line 7; page 1283, column 2, lines 22-35; page 1284, column 1, line 13 to column 2, line 5; figure 5 (cited in the application)	1-38	Y	IEEE Transactions on Electron Devices, volume ED-29, no. 10, October 1982, New York (US) D.E. Wortman et al.: "Improved OROTRON performance in the 50- to 75-GHz frequency region", pages 1639-1640, see abstract; figure 1	1-38	Y	Nuclear Instruments & Methods, volume 204, no. 2/3, January 1983, Amsterdam (NL)	
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Y	Nuclear Instruments & Methods, volume 204, no. 2/3, January 1983, Amsterdam (NL)													
<div style="display: flex; justify-content: space-between;"> <div style="width: 48%;"> <p>¹⁰ Special categories of cited documents:</p> <p>"A" document defining the general state of the art which is not considered to be of particular relevance</p> <p>"E" earlier document but published on or after the international filing date</p> <p>"L" document which may throw doubts on priority claim(s) or which is cited to establish the publication date of another citation or other special reason (as specified)</p> <p>"O" document referring to an oral disclosure, use, exhibition or other means</p> <p>"P" document published prior to the international filing date but later than the priority date claimed</p> </div> <div style="width: 48%;"> <p>"T" later document published after the international filing date or priority date and not in conflict with the application but cited to understand the principle or theory underlying the invention</p> <p>"X" document of particular relevance; the claimed invention cannot be considered novel or cannot be considered to involve an inventive step</p> <p>"Y" document of particular relevance; the claimed invention cannot be considered to involve an inventive step when the document is combined with one or more other such documents, such combination being obvious to a person skilled in the art.</p> <p>"A" document member of the same patent family</p> </div> </div>														
IV. CERTIFICATION <table style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 50%; border-bottom: 1px solid black; padding: 5px;">Date of the Actual Completion of the International Search</td> <td style="width: 50%; border-bottom: 1px solid black; padding: 5px;">Date of Mailing of this International Search Report</td> </tr> <tr> <td style="border-bottom: 1px solid black; padding: 5px;">6th January 1987</td> <td style="border-bottom: 1px solid black; padding: 5px;">06 FEB 1987</td> </tr> <tr> <td style="border-bottom: 1px solid black; padding: 5px;">International Searching Authority</td> <td style="border-bottom: 1px solid black; padding: 5px;">Signature of Authorized Officer</td> </tr> <tr> <td style="padding: 5px;">EUROPEAN PATENT OFFICE</td> <td style="padding: 5px;">M. VAN MOL </td> </tr> </table>			Date of the Actual Completion of the International Search	Date of Mailing of this International Search Report	6th January 1987	06 FEB 1987	International Searching Authority	Signature of Authorized Officer	EUROPEAN PATENT OFFICE	M. VAN MOL				
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International Searching Authority	Signature of Authorized Officer													
EUROPEAN PATENT OFFICE	M. VAN MOL													

III. D DOCUMENTS CONSIDERED TO BE RELEVANT (CONTINUED FROM THE SECOND SHEET)		
Category *	Citation of Document, with indication, where appropriate, of the relevant passages	Relevant to Claim No
	H. Bilokon et al.: "Coherent Bremsstrahlung in crystals as a tool for producing high energy photon beams to be used in photoproduction experiments at CERN SPS", pages 299-310, see abstract; table 1	21-24,31
	--	
Y	Applied Physics Letters, volume 44, no. 7, April 1984, New York (US) A.E. Kaplan et al.: "Extreme-ultraviolet and X-ray emission and amplification by nonrelativistic electron beams traversing a superlattice" pages 661-663, see abstract	25-27
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A	US, A, 2634372 (W.W. SALISBURY) 7 April 1953, see claim 1; figures (cited in the application)	1
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A	Journal of Applied Physics, volume 50, no.1, January 1979, New York (US) J.M. Wachtel: "Free electron lasers using Smith-Purcell effect", pages 49-56, see abstract	1
	--	
A	IEEE Journal of Quantum Electronics, volume QE-19, no. 3, March 1983 New York (US) M.A. Piestrup et al.: "The prospects of an X-ray free electron laser using stimulated resonance transition radiation", pages 357-364, see abstract; page 363, column 2, lines 33-38	1
